

SARC = *Semi Analytical Recursive Convolution*

This simulation approach is dedicated to *Linear Time Invariant* analog circuit (**LTI**)

There is *no convergence* nor enigmatic user setup parameters (*since there is no parameter !*)

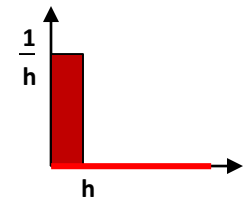
The *step calculation* is directly the result of *matrix arithmetic sequential operations*

Moreover, an *estimation* of the *step interpolation error* can be evaluated as a possible *metric* of the simulation *quality*

Inductances and *Capacitances* values can be changed “*on the fly*”

thanks to the algorithm conservation of the *flux* or the *charge* at the *instant* of the changes (called *percussion*)

Accurate *impulsional response* can be simulated (using the input



SARC is able to return to the user the *numerical values of the poles* as well as the *overall* value of the *energy* accumulated within the L and C

Finally, symbolic *Laplace transfer functions* of the circuit can also be returned

Maxima output syntax

OUTPUTS(... , f(*component*) , ...)

cumulated step interpolation error

cumulated Max step interpolation error

<i>function</i> <i>component</i>	V	I	cV	cI	eV	eI	ecV	ecI	mV	mI	mcV	mcI
nodes	✓				✓				✓			
V , I , R , L , C	✓	✓			✓	✓			✓	✓		
E , G	✓	✓	✓		✓	✓	✓		✓	✓	✓	
H , F	✓	✓		✓	✓	✓		✓	✓	✓		✓

control source

Moreover, the following declaration is also possible in **OUTPUTS(...)**

J() that stands for overall L & C *stored energy calculation* (Joules)

The following *user request* can be added in the *Maxima* circuit description

PRINTPOLES(N) ;

 print (*up to N times*) the **POLES** of the system matrix “**A**”

During **SARC** execution, whenever some **R** , **L** or **C**
are “*percuted*” the “**A**” matrix gets modified, and its **POLES** printed as

real part

imaginary part

= *frequency*

that is more convenient than

the theoretical pulsation ω ($\Rightarrow 2 \pi f$)

AKA(C_{common} , C1 , C2 , C3) ;

AKA(R_{common} , “5E-3” , R1 , R2 , R3) ;

AKA(R_{common} , R1 , R2 , R3 , “1500”) ;

SARC is based on a (*semi*) *analytical* approach

⇒ it does not require any “*rule of thumb options*” to control its *execution & accuracy*

However, at **Maxima** level , the following “*modes*” can be selected

rubmode (0 by default) to partially / totally disable the update of the *output vector* with the information at **t+**

rubmode : 1 ; “omit” the update BUT only in case of L and/or C percussion (*glitch < h* not shown)

rubmode : 2 ; constantly “omit” the update (thus *immediate STEP changes* NEVER shown)

It should be noted that, in any cases, the rest of the simulation remains accurate (except that *outputs* at **t+** may be hidden)

degenmode (true by default) to enable / disable the *degeneration* solver

degenmode : false ; *disable* the solver
in case of degeneration, **RESISTORS** must be inserted in the **NETLIST** to resume execution

sdegenmode (true by default) to enable / disable the *source degeneration* solver

sdegenmode : false ; *disable* the solver
in case of degeneration, **RESISTORS** must be inserted in the **NETLIST** to resume execution

DEGENERATION can result from **2** different circuit configurations



a **shared voltage across** a group of capacitors
(or a **common current** for inductors)

examples:

// capacitors **serial inductors** **capacitors** connected as polygons ...



a **common current** constraining **flawlessly** a group of capacitors
(or a **shared voltage across** inductors)

This configuration is the same that reports **floating nodes** during **SPICE** analysis

examples:

serial capacitors **// inductors**

a third hassle exists that could also complicate the symbolic determination of matrix "**A**"



the first configuration but with an **input** (or **controlled source**) **as part of the group**

for **capacitors** with **driving voltage** or **inductors** with **driving current** this results in
a **Dirac transfer** of energy to a **pure reactance bridge** (due to the absence of any **real world** time constant)

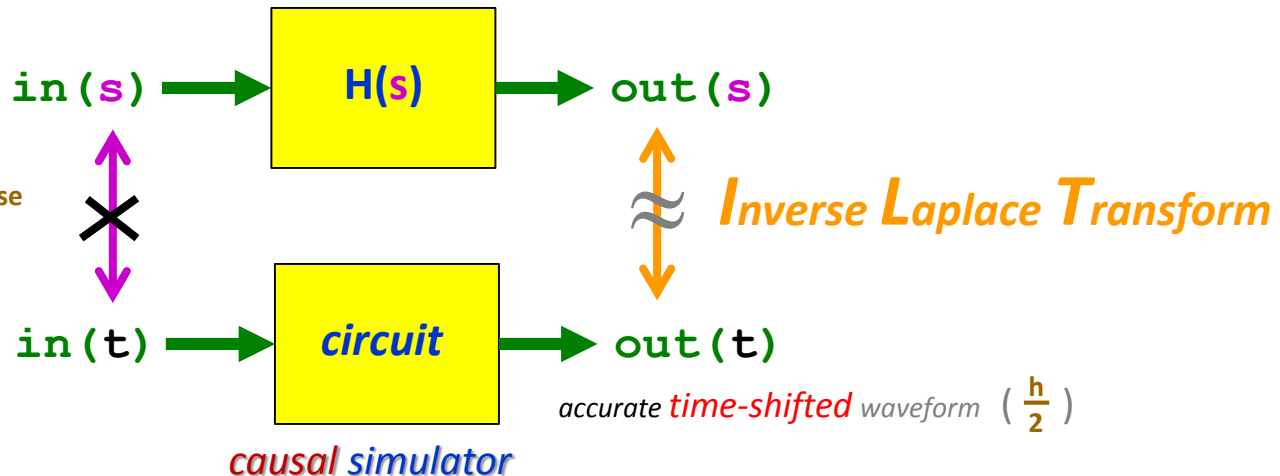
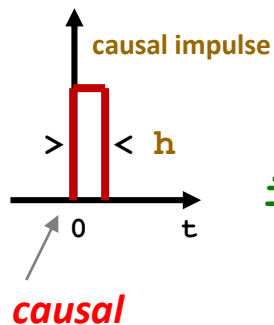
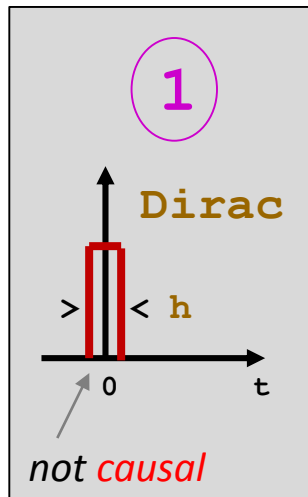
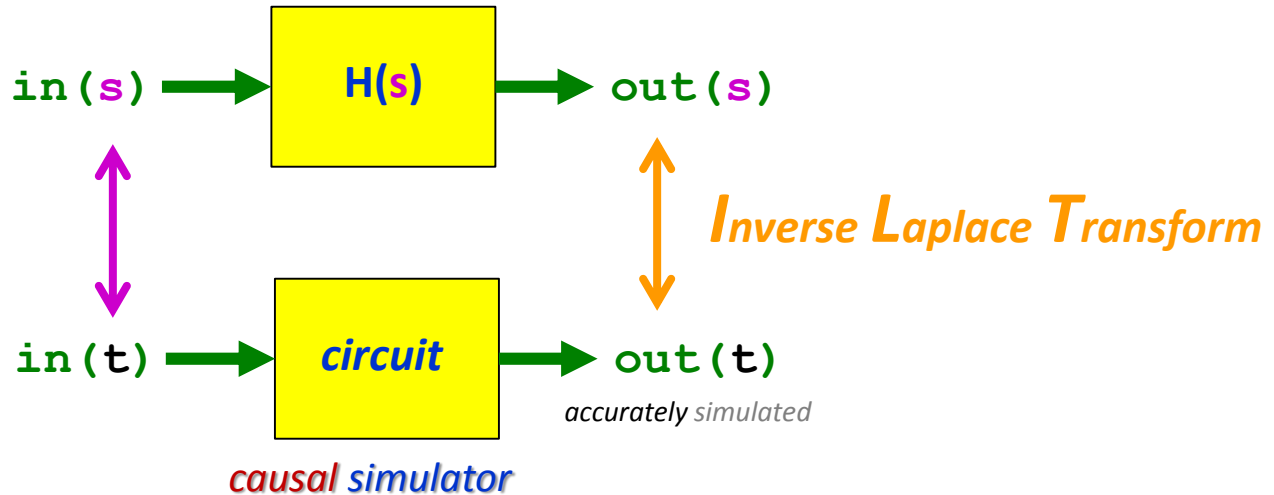
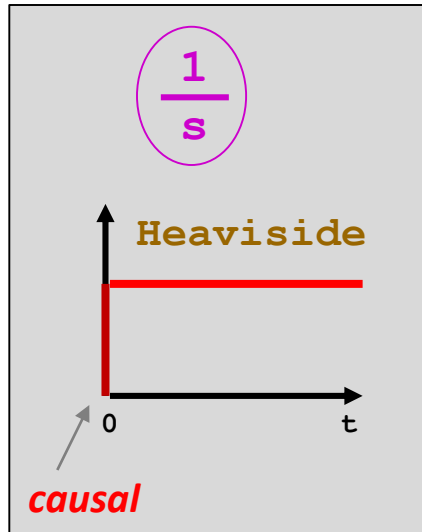
Unlike the usual case , it should be noted that the **state variables** associated to those bridges cannot be
confounded with the **V** (or **I**) of their corresponding components (since a **direct source contribution** also exists)

IDEALISATION

<=>

is the circuit able to generate the **burst** ??? does the reactance able to survive to such **burst** ???

Validation: *simulation* versus Laplace

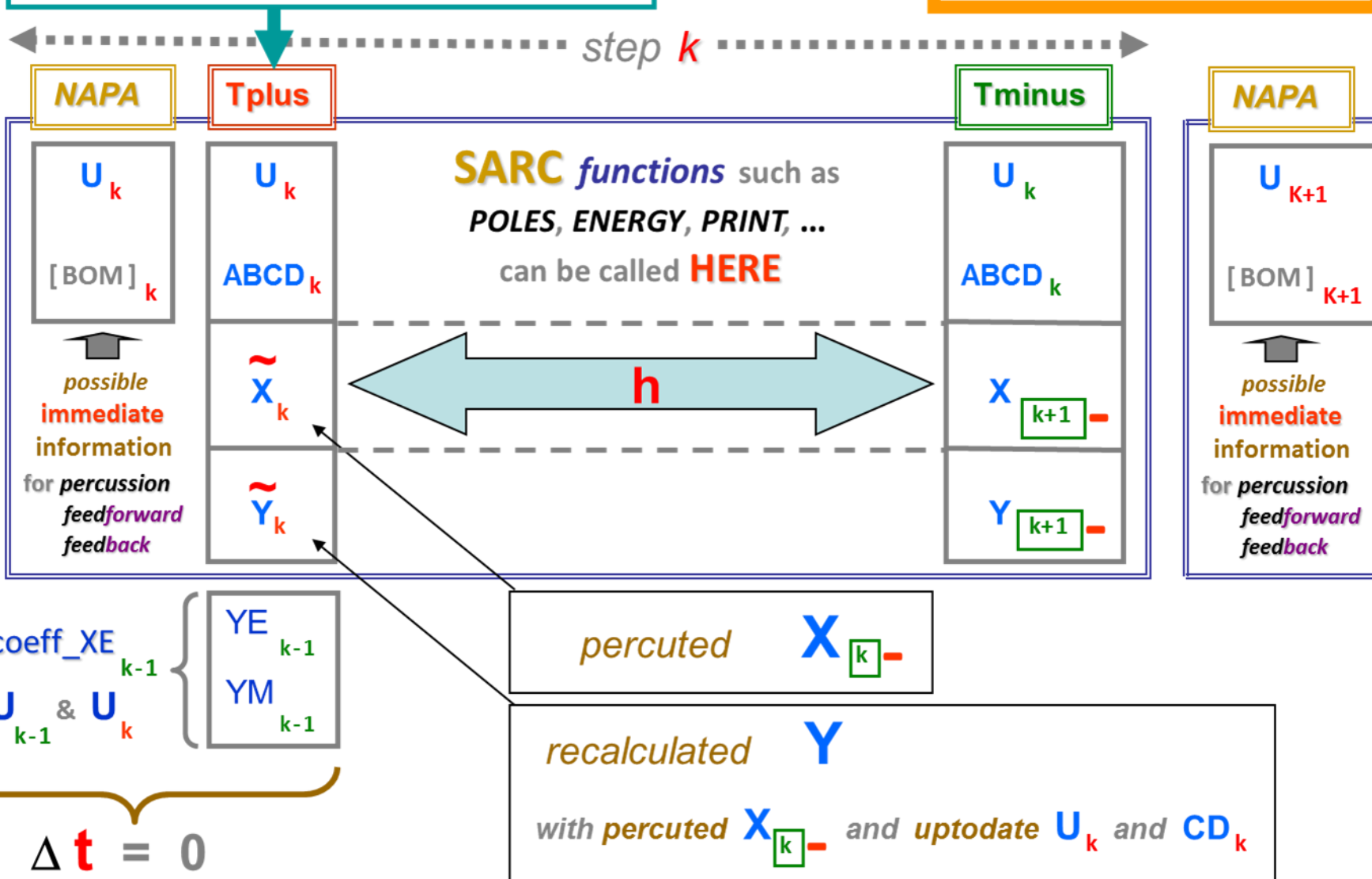


rubmode 0 t+ accurate (default)
 1 t+ accurate except "AT" L&C percussion
 2 t+ "immediate STEP changes" NEVER shown

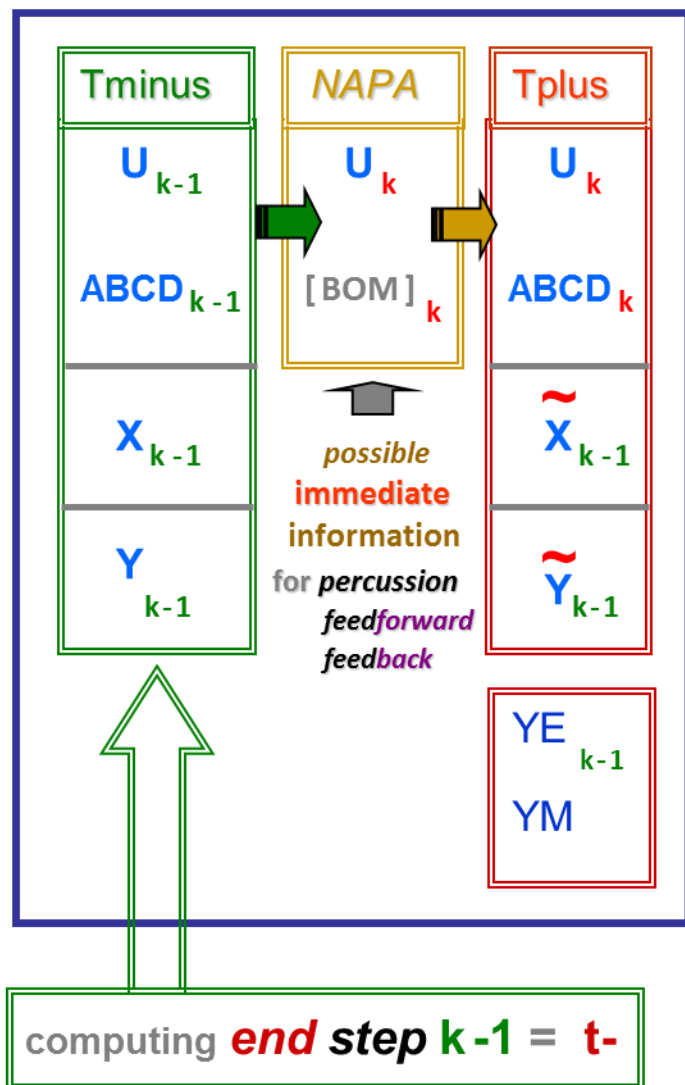
This option does NOT change the accuracy of the NEXT steps

glitch < h
 not shown

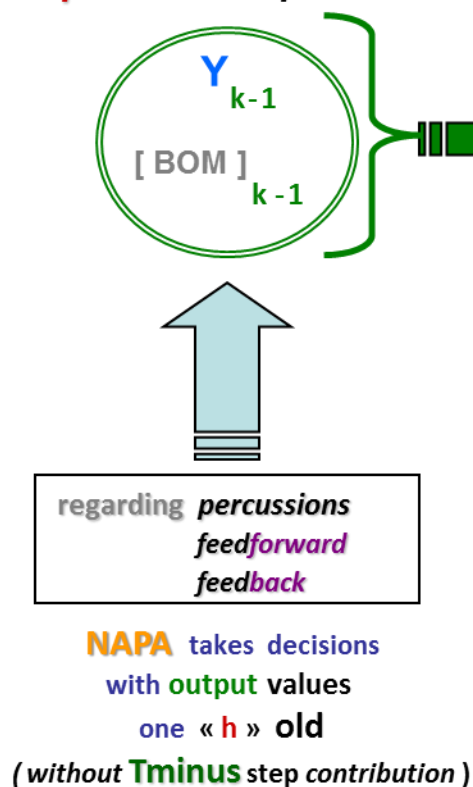
ideal SARC
scheduling



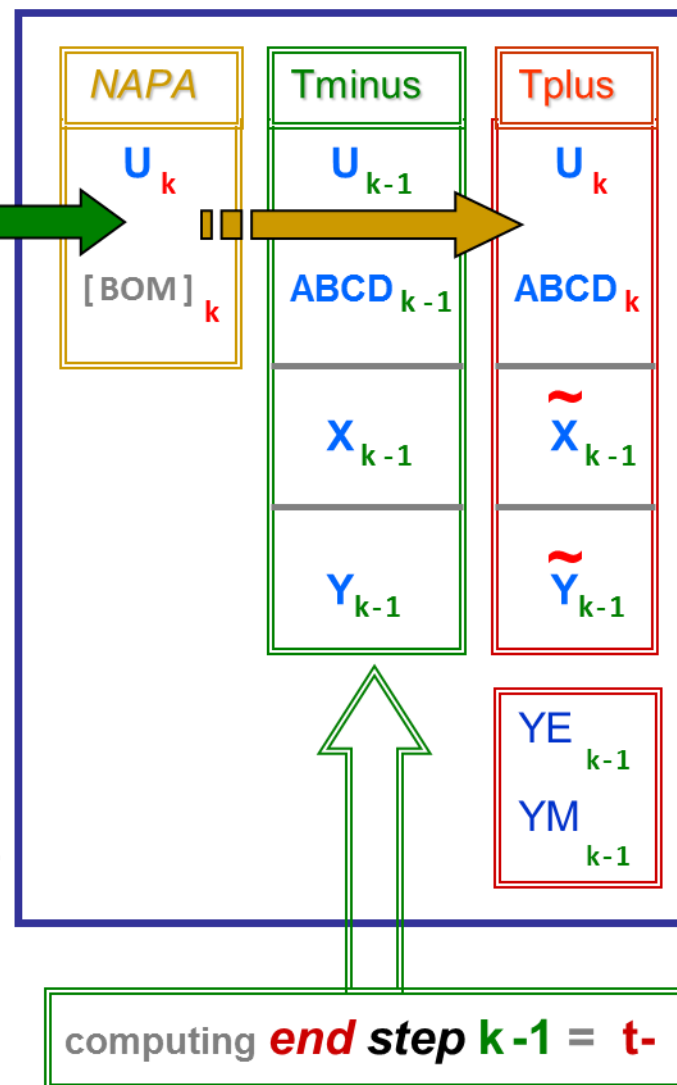
ideal **SARC** scheduling



values of beginning previous step



current **NAPA** implementation



FEEDBACK & FEEDFORWARD

SARC

$$e^{ah} x(t-h) + b e^{at} \int_{t-h}^t e^{-a\tau} \text{interpolation}(\tau) d\tau$$

$U[t-h]$

SOB

$Y[t-]$

interpolation interval

step

$t-h$

t

feedback equations

at " t " are based on

OUTPUTS[$t-$]

resulting from the

most recent convolution

OUTPUTS[$t-$] **update** in case of

feedforward

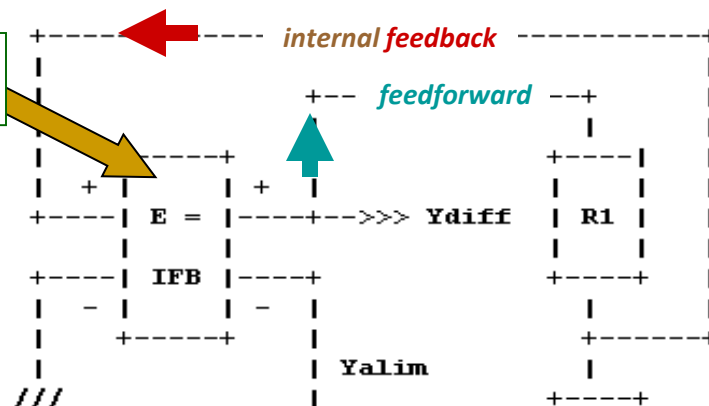
(matrix " D " not null)

and
or

percussion

(but conditionally to *rubmode*)

percussion
internal feedback



no feedback (IFB = 0) $H = \frac{R_2}{R_1 + R_2}$

feedback $G = \frac{H}{1 + H} = \frac{R_2}{R_1 + (1 - IFB) R_2}$

IFB = - 1 $G = \frac{R_2}{R_1 + 2 R_2}$

Yref Y_{test1} Y_{test2}

REF $EFB = ()$
equation $()$
triggeedd by $()$
 Y_{test1}

STEP size h = 1 s
SIMU length = 8 s
Tpercussion = 4 s

```

----- at init ----- IFB = -1.0  R1 = 4k  R2 = 2k  ( ==>> G = 1/4 )
but  Ytest1 >= 1        ==>>> IFB = 0   R1 = 1k  R2 = 1k  ( ==>> G = 1/2 )

----- at init ----- EFB = 0.25 * t
but  Ytest1 >= 1        ==>>> EFB = 0.50 * t

----- at init ----- REF = 0.25 * t
but  t >= Tpercussion ==>>> REF = 0.50 * t

```

external feedback

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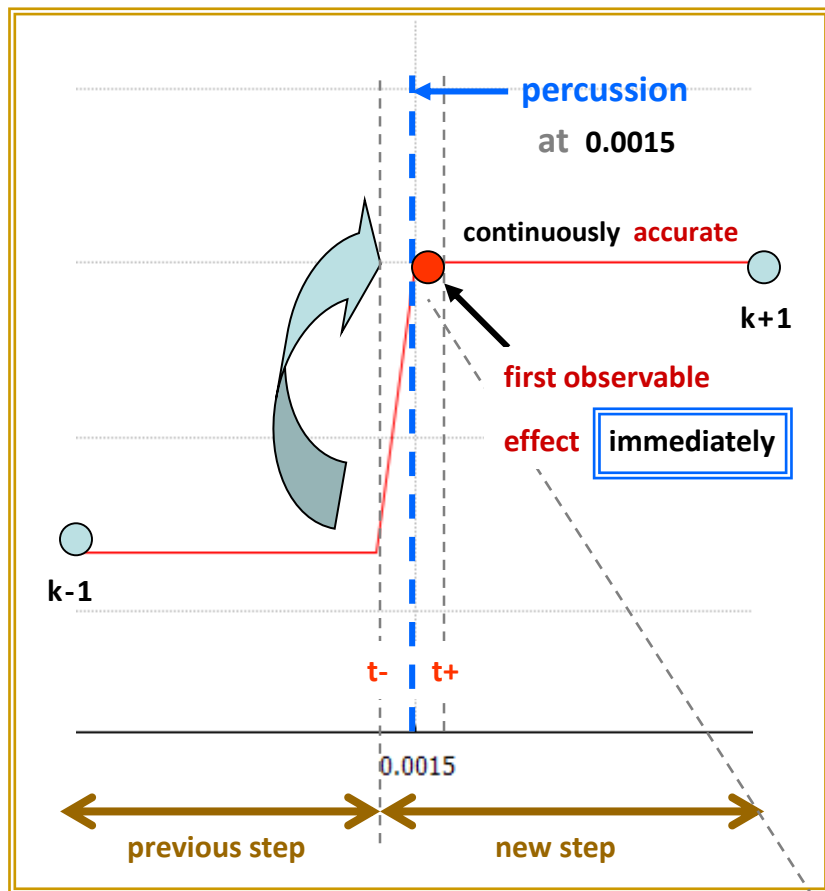
rubmode : 0 ;

NETLIST( /*-----*/
[ V , BAT , Yalim , Gnd ] ,
[ E , IFB , Ydiff , Yalim , Ytest1 , Gnd ] ,
[ R , R1 , Ydiff , Ytest1 ] ,
[ R , R2 , Ytest1 , Gnd ] ,
/*-----*/
[ V , EFB , Ytest2 , Gnd ] ,
/*-----*/
[ V , REF , Yref , Gnd ] ,
/*-----*/ ) ;

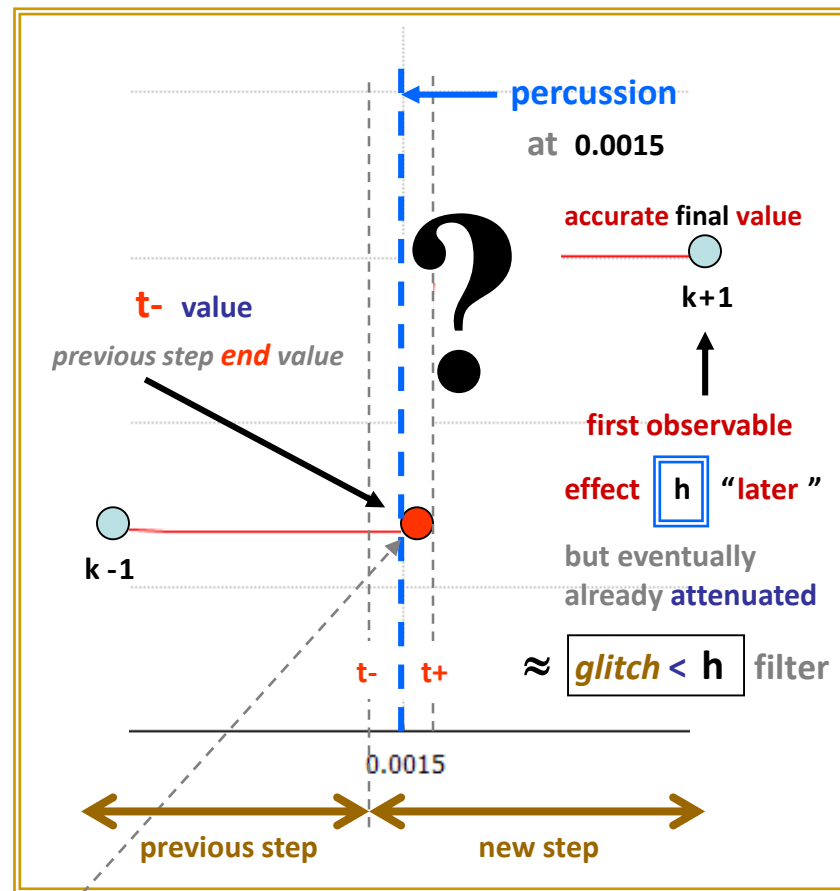
OUTPUTS( V(Yalim) , V(Ydiff) , V(Ytest1) , V(Ytest2) , V(Yref) ) ;

```

$\text{rubmode} = 0$ (default)

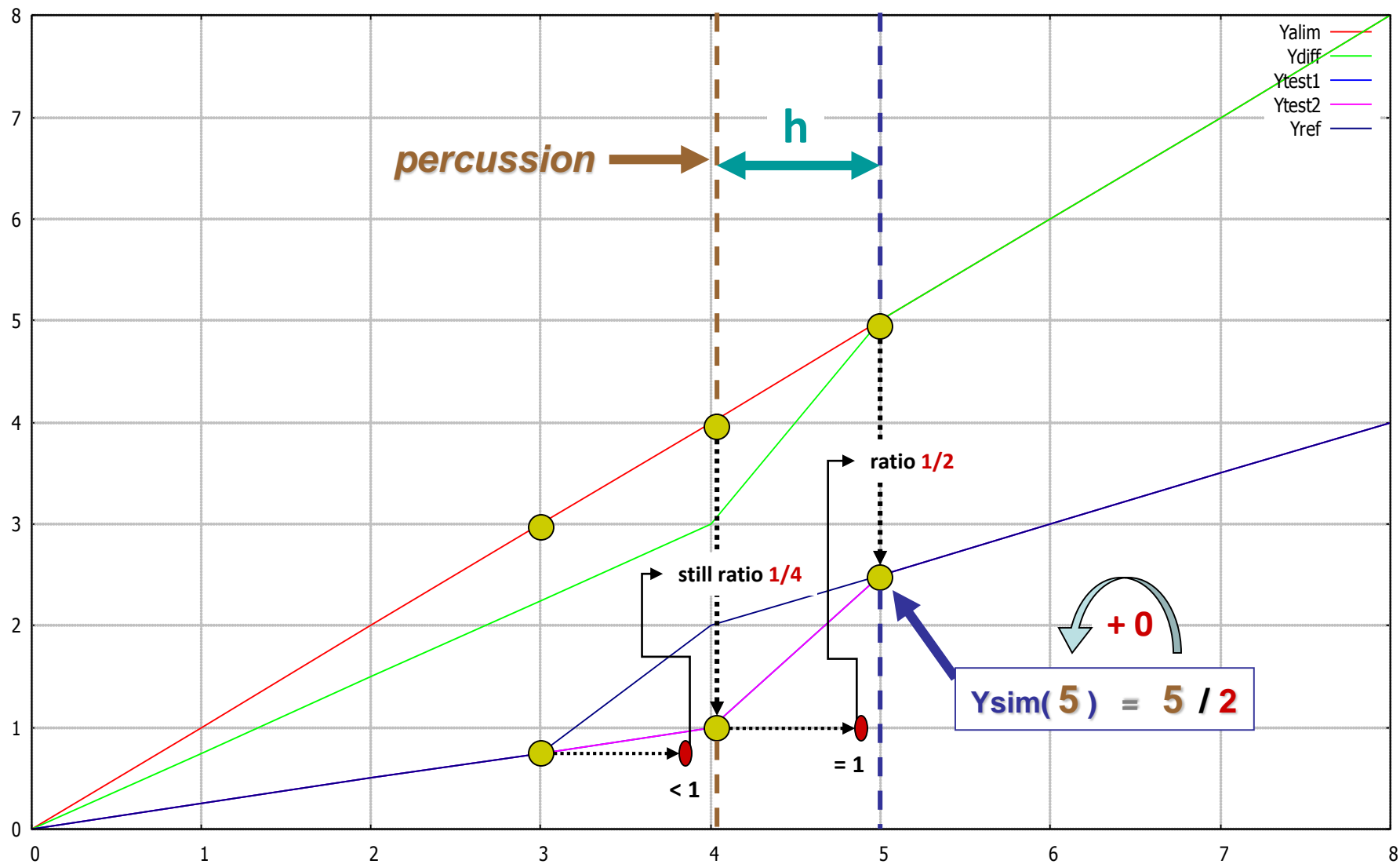


$\text{rubmode} \neq 0$



warning: in *rubmode* (when no explicit NAPA delay) the overall simulation waveform appears just *shifted in time*

(*rubmode* = 0)



(*rubmode* = 2)

